

Mechanistic Machine Learning for Engineering and Applied Science

Part I: Introduction and overview

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What is learning?

“Learning is any process by which an entity improves performance from experience.” - Herbert Simon

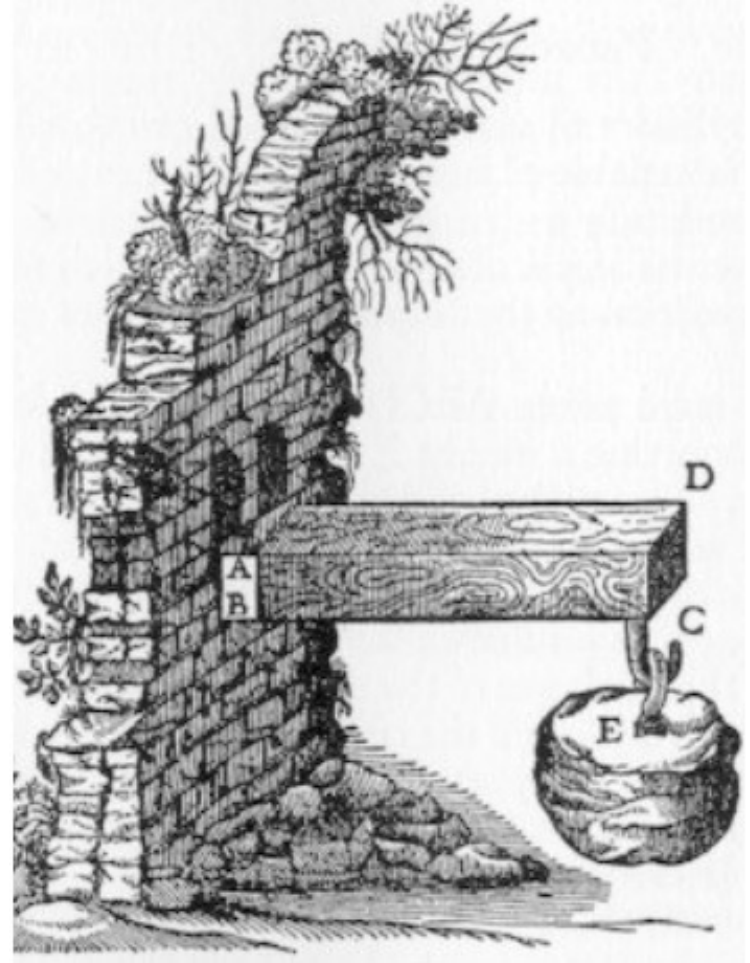
Example – The ability to deduce $F=ma$ by observing the trajectory of the apple falling from the tree.

What is machine learning?

Machine Learning is the study of algorithms that

- improve their performance P
- at some tasks T
- with experience E .

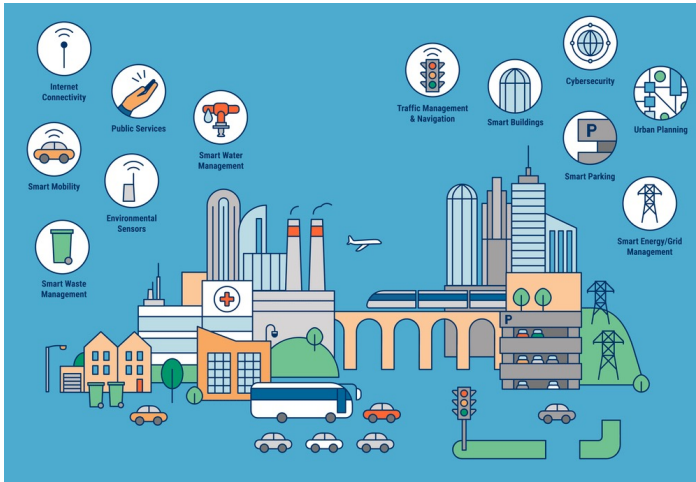
A well-defined learning task is given by $\langle P, T, E \rangle$.



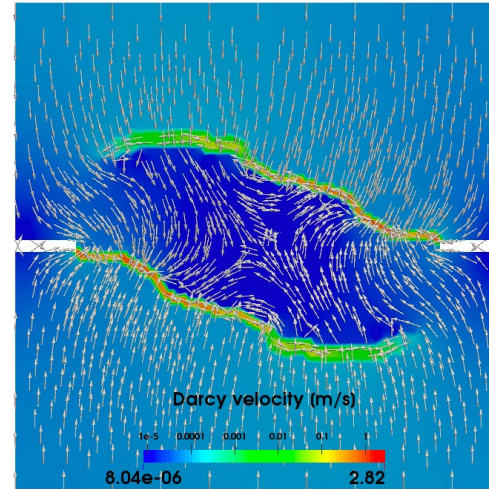
Why Machine Learning?

- Automating automation
- Getting computers to program themselves
- Writing software could be the bottleneck
- Let the data do the work instead!

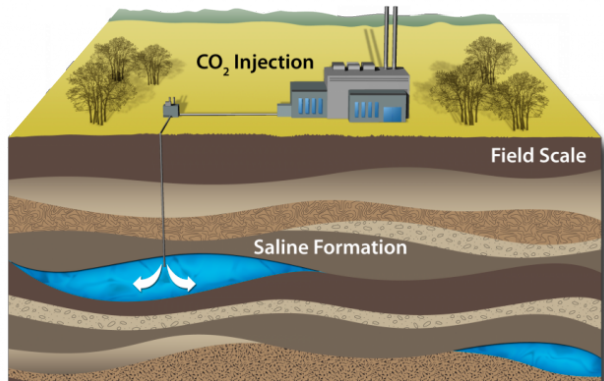
Example Applications in Engineering



Smart City



Material modeling



CO₂ geological storage



Earthquake predictions

Promises?

- “A breakthrough in machine learning would be worth ten Microsofts” (Bill Gates, Chairman, Microsoft)
- “Machine learning is the next Internet” (Tony Tether, Director, DARPA)
- Machine learning is the hot new thing” (John Hennessy, President, Stanford)
- “Machine learning is going to result in a real revolution” (Greg Papadopoulos, CTO, Sun)

BUT

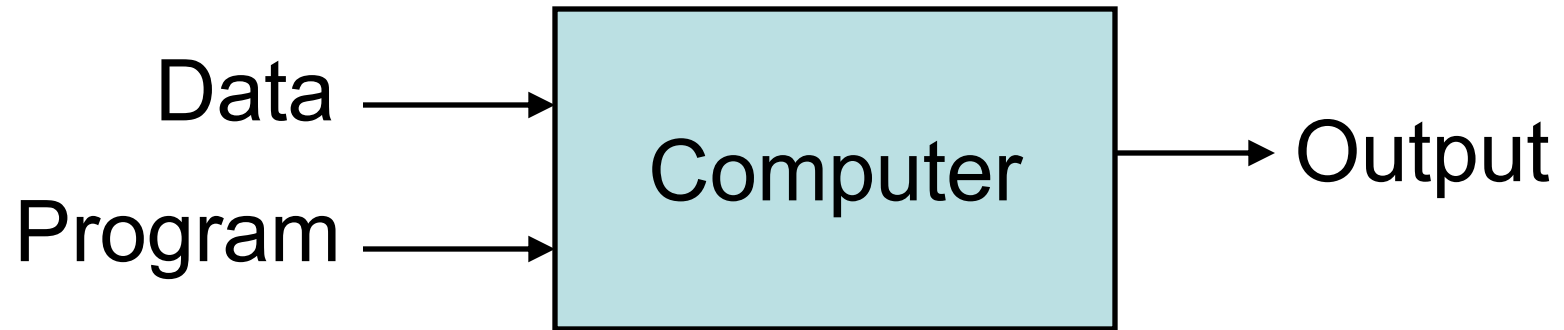


Elon Musk 
@elonmusk

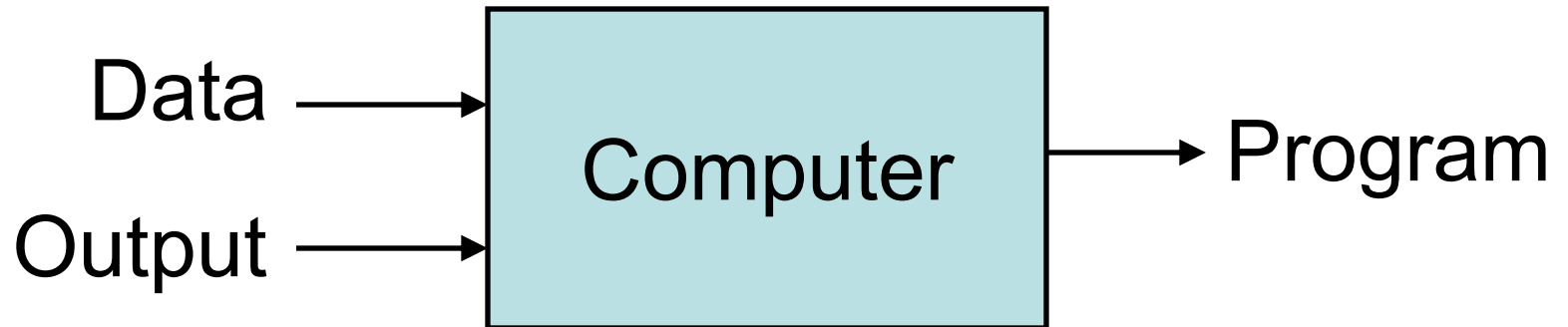


If you're not concerned about AI safety, you should be.
Vastly more risk than North Korea.

Traditional Programming



Machine Learning



Example: Rock Scissors Paper Game

Traditional Approach – explicitly programming the rules

```
switch (action)
{
  case "rock" :
    reaction = "paper"; break;
  case "scissors":
    reaction = "rock"; break;
  default:
    reaction = "scissors"
}
```

ML Approach – implicitly "learning" the rules from the patterns

Given: History of game played, e.g.

Game 1: Input = rock-scissors, output = loss
Game 2: Input = scissors-paper, output = loss
Game 3: Input = rock-paper, output = win
...etc

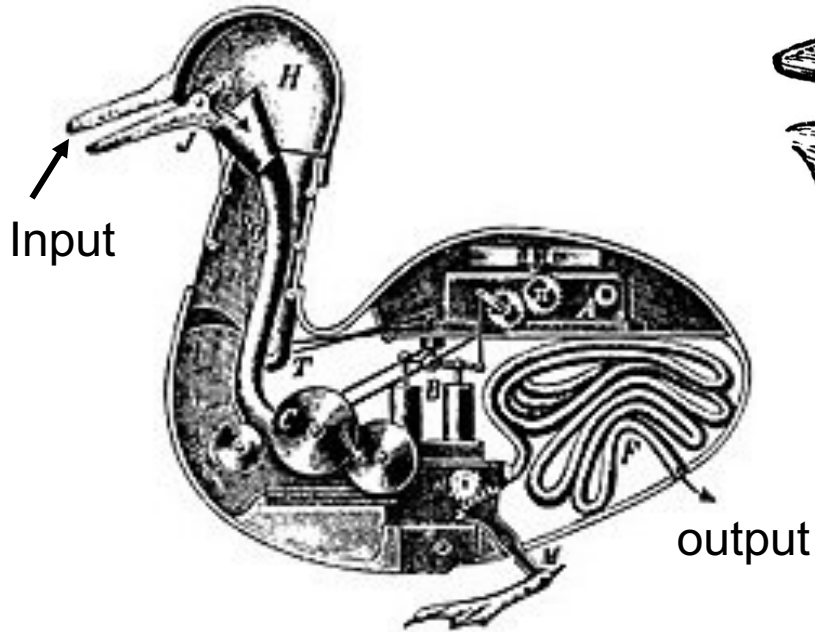
Computer then "training" the AI by providing the data to the AI

AI learns the "rule" and make predictions

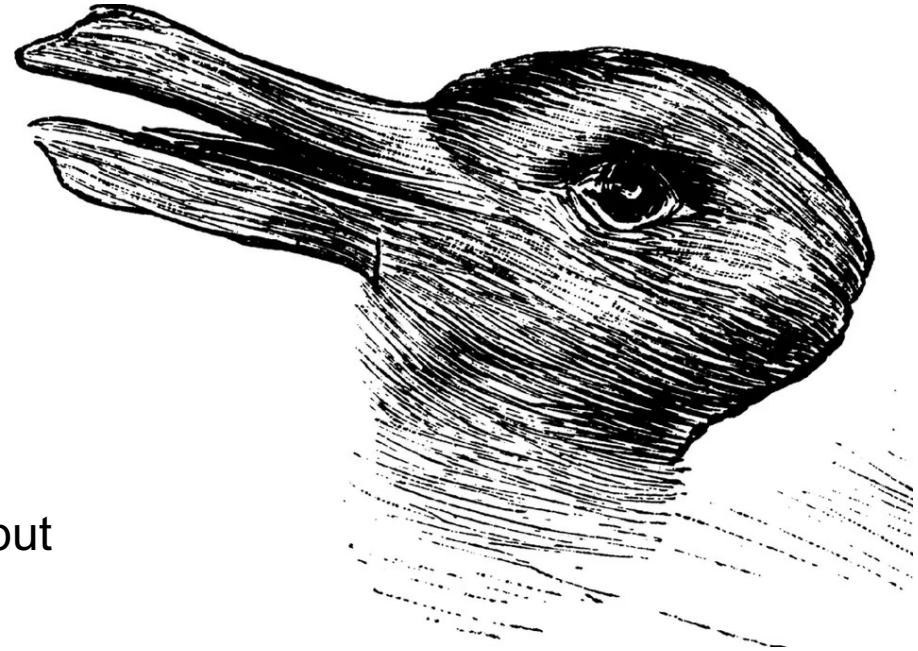
The key difference is that the rule has never been explicitly programmed

Example: “Seeing that” vs. “seeing as”

Rationale of Predictions: External behaviors vs. internal properties



Canard Digérateur (1741)



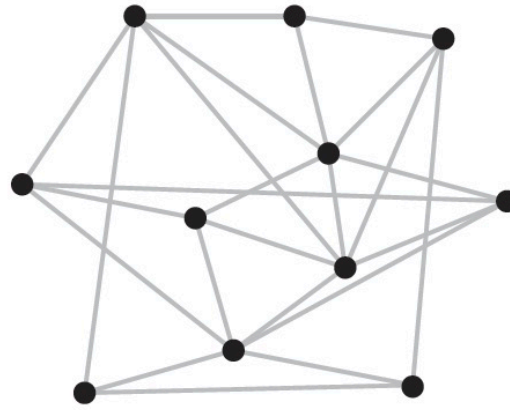
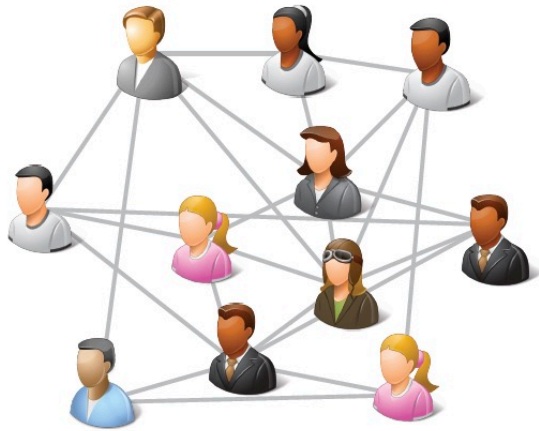
Duck-rabbit (1892)

ML in a Nutshell

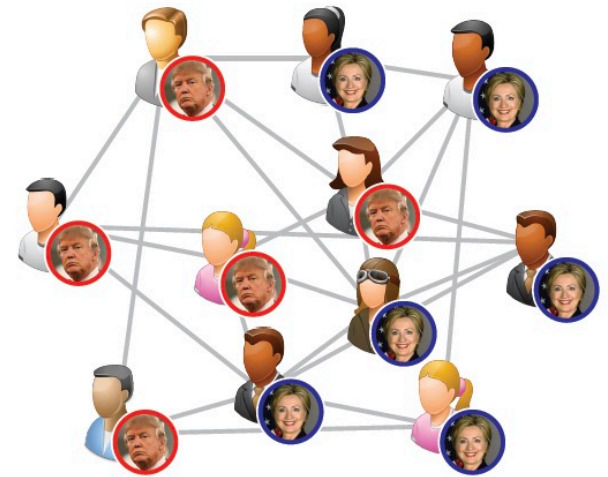
- Every machine learning algorithm has three components:
 - **Representation**
 - **Evaluation**
 - **Optimization**

Example: Data Representation

Consider descriptors of data as the ingredients for theory

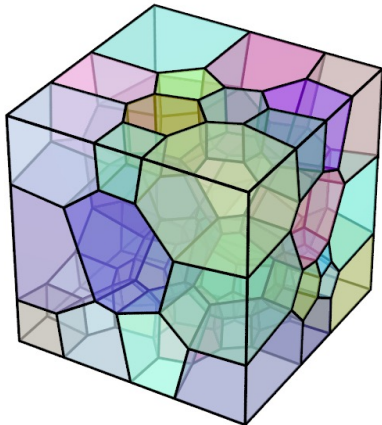
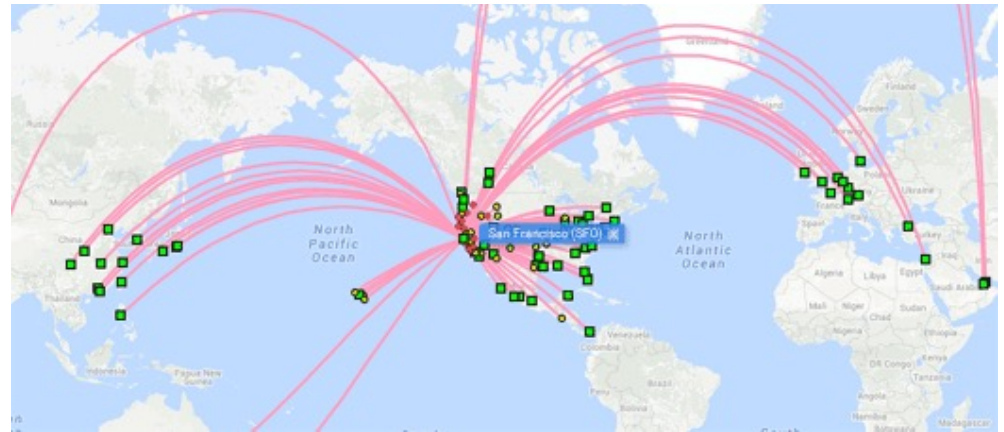
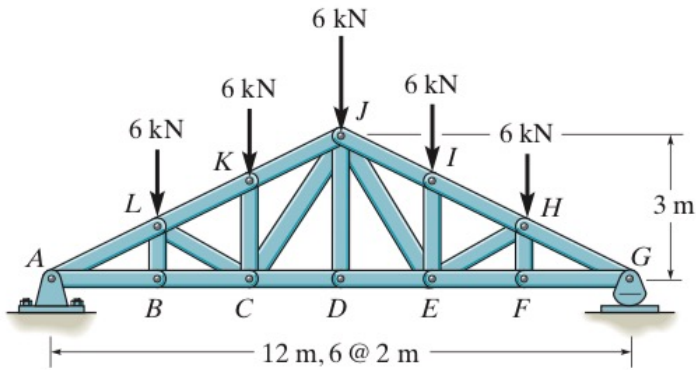


Domain structure

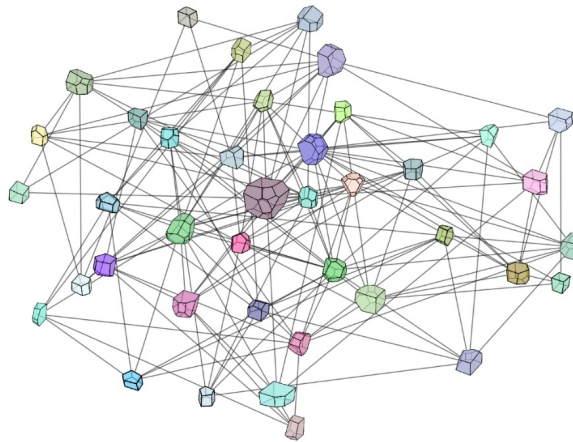


Social network

Example for civil engineering and engineering mechanics

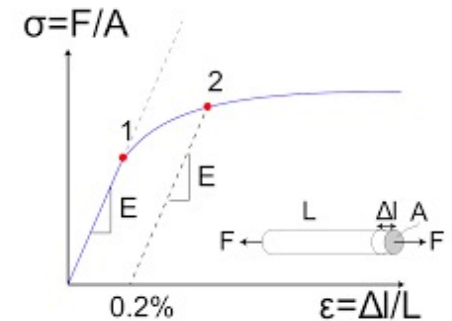


Polycrystal RVE



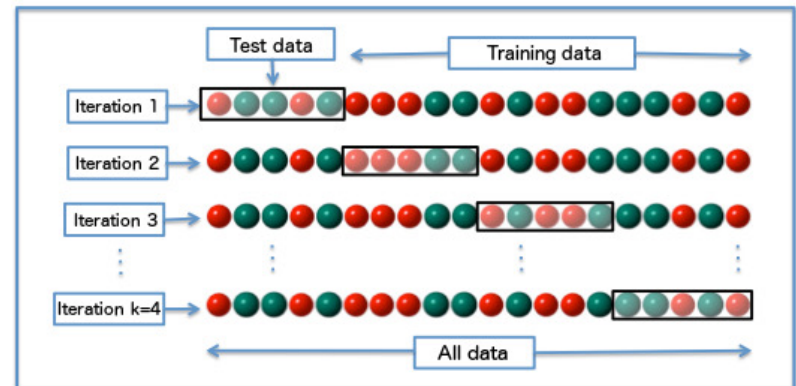
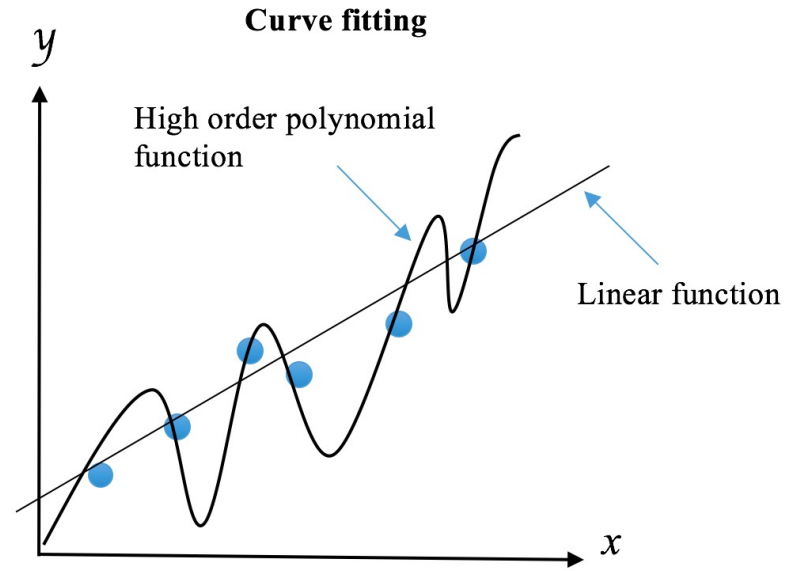
Node-weighted undirected
crystal connectivity graph

- Constitutive law generation from non-Euclidean grid data



Evaluation

- Accuracy
- Precision and recall
- Squared error
- Likelihood
- Posterior probability
- Cost / Utility
- Margin
- Entropy
- K-L divergence
- Etc.

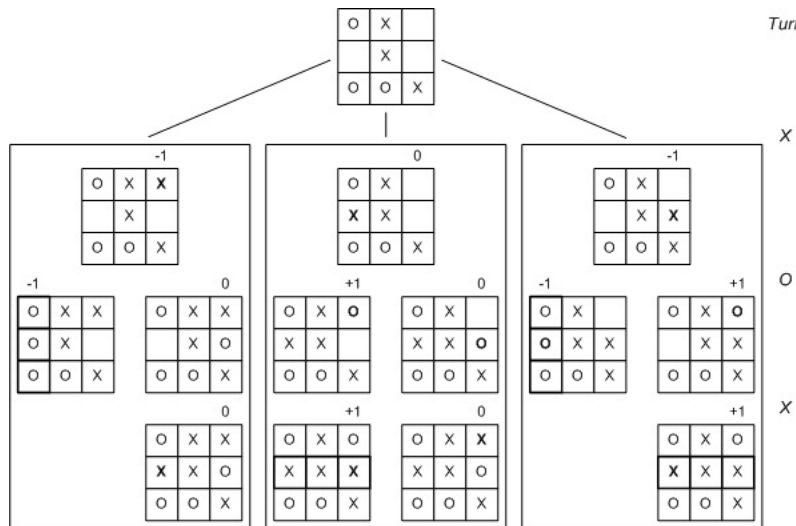


Optimization

- Combinatorial optimization
 - E.g.: Greedy search
- Convex optimization
 - E.g.: Gradient descent
- Constrained optimization
 - E.g.: Linear programming

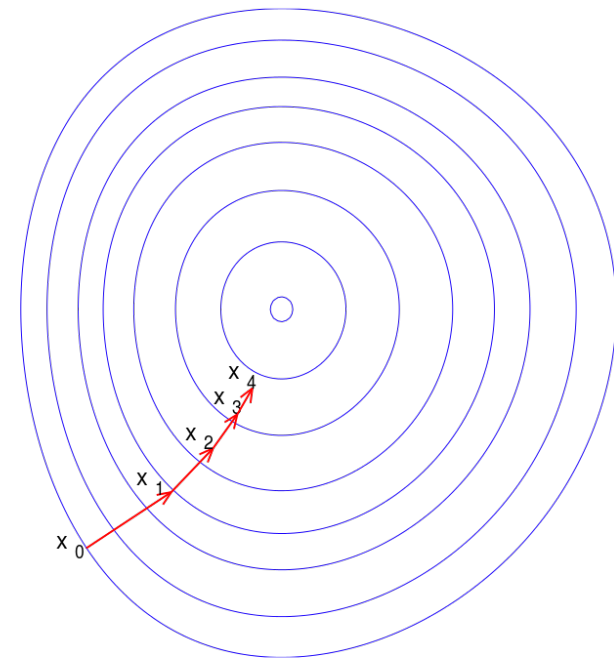
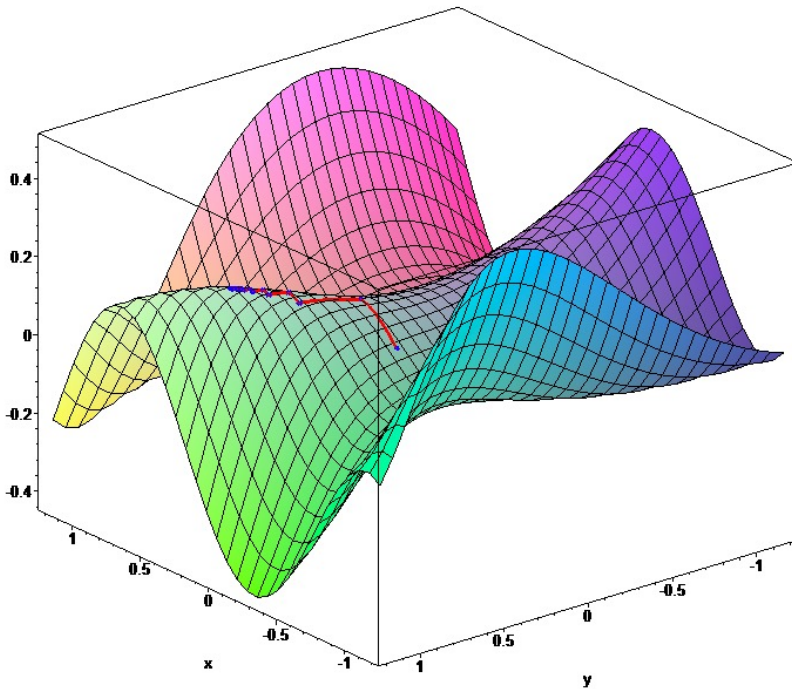
Combinatorial Optimization

- How to determine elements of a set or n-tuple that maximize an objective function?

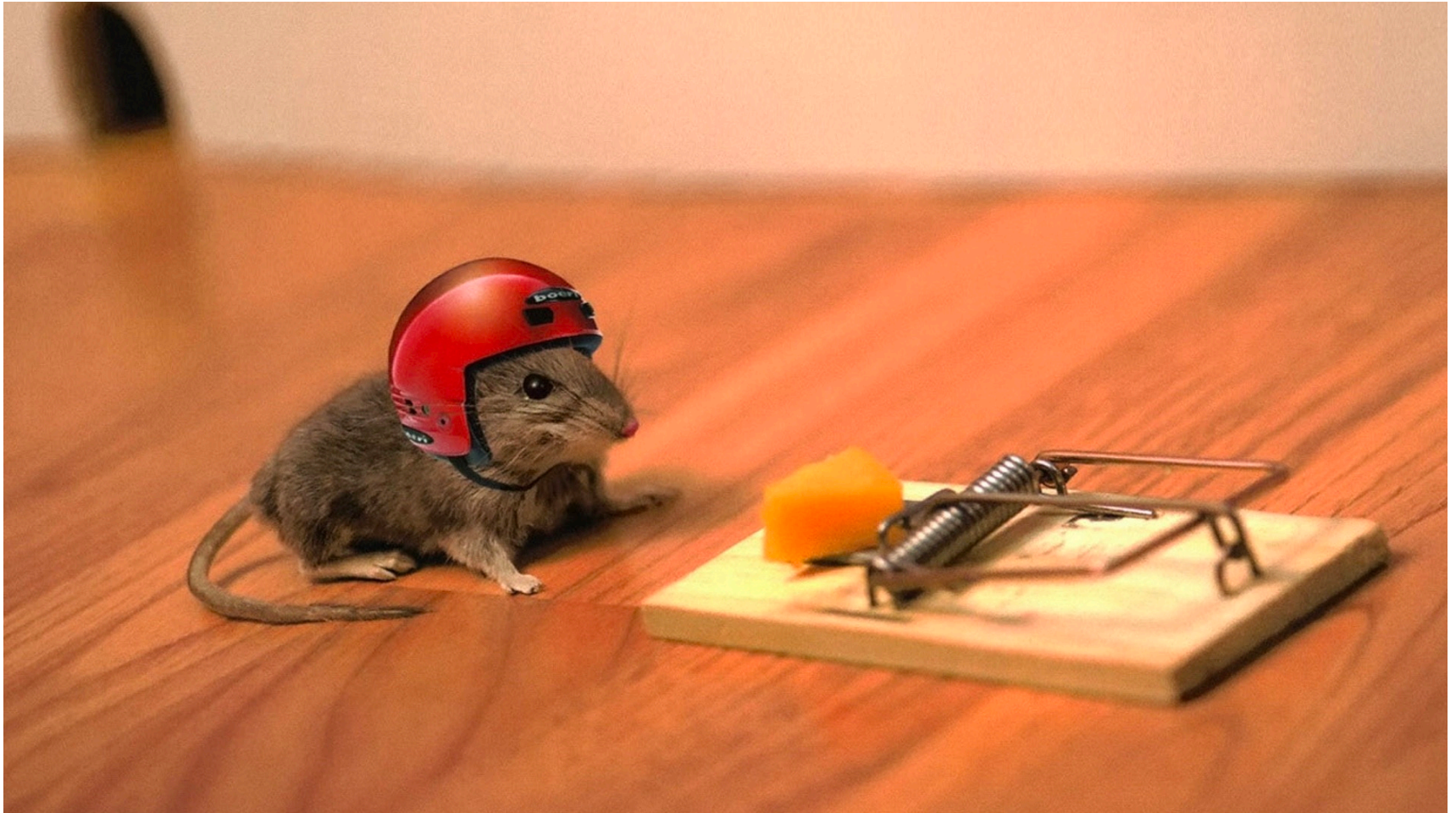


Convex and constrained Optimization

- How to a point in a parametric space that maximize one or multiple objective functions?



Exploitation vs exploration

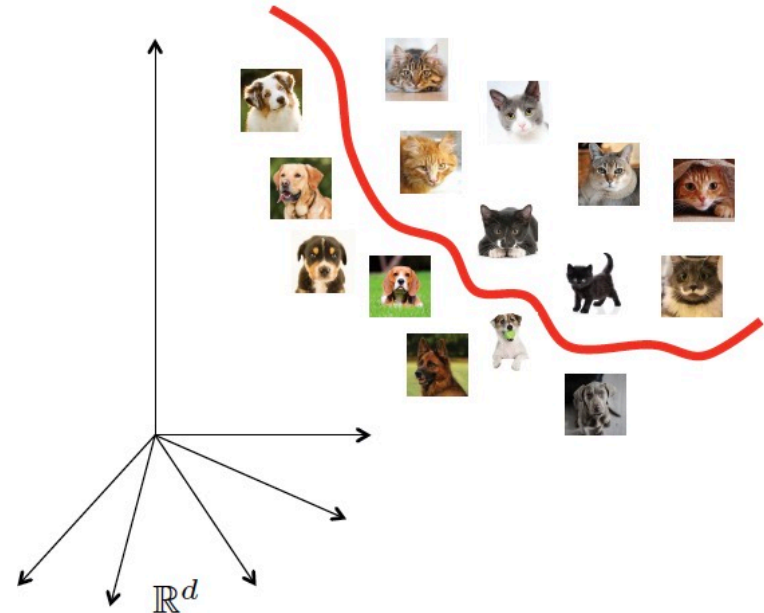


Major branches of machine learning

- **Supervised learning**
 - Rule induction from input/output pairs
 - Learn with labeled data
- **Unsupervised learning**
 - Dimensional reduction
 - Data compression
 - No output required
- **Reinforcement learning**
 - Markov decision process
 - Agent interact with environment
 - Need reward from environment influence actions

Supervised Learning

- **Given** examples of a function $(X, F(X))$
- **Predict** function $F(X)$ for new examples X
 - Discrete $F(X)$:
Classification
 - Continuous $F(X)$:
Regression
 - $F(X) = \text{Probability}(X)$:
Probability estimation



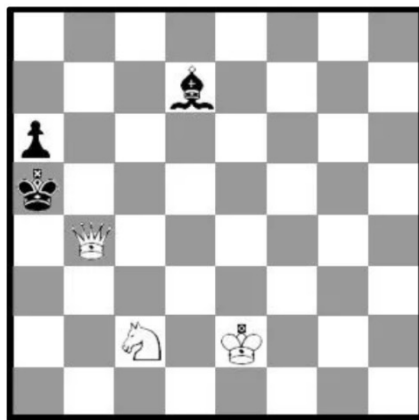
Example: Classification Problems?
Input: pictures of dogs and cats
Output: The label “dog” or “cat”

Reinforcement learning and Game

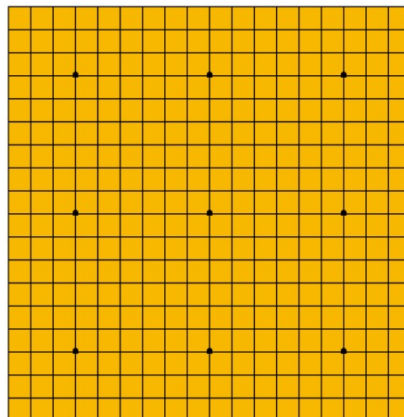
Chess



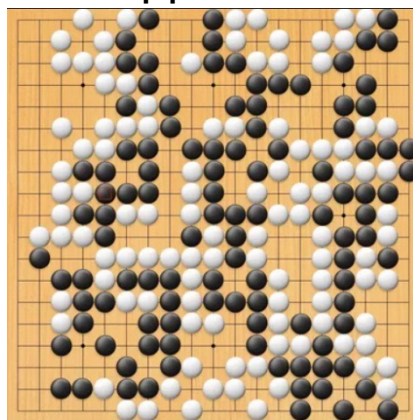
Move pieces to put the opponent's king in "checkmate"



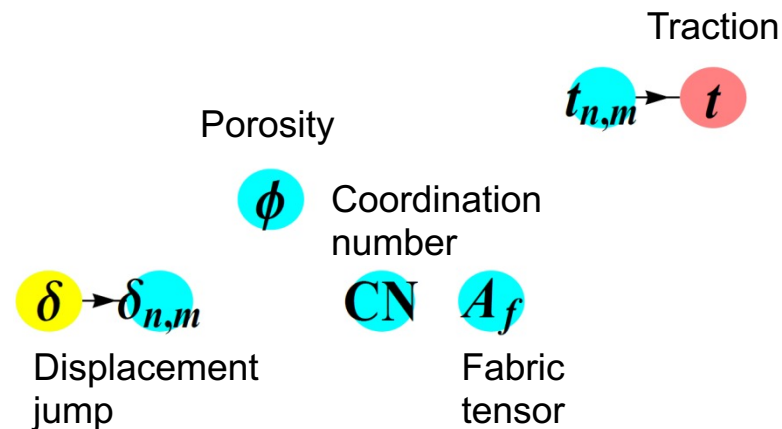
Go Game



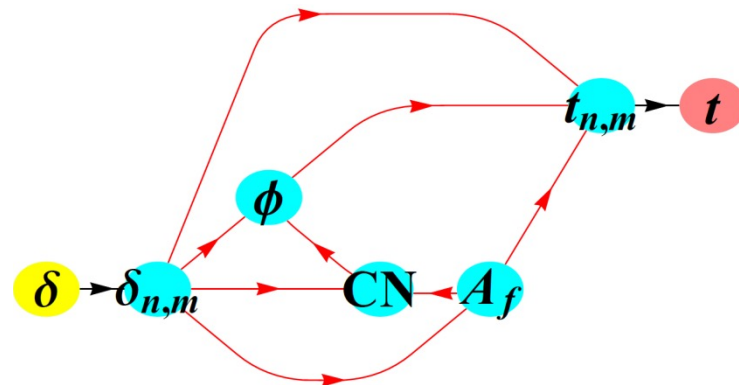
Place pieces to control more territory than your opponent



Meta-modeling Game



Connect edges to generate optimal internal information flow of constitutive models



Applications in Engineering

- Transportation Engineering
- Engineering Mechanics
- Topological optimization
- Predictive modeling
- Architecture materials

And countless more